

The Four Color Theorem

How many different colors are sufficient to color the countries on a map in such a way that no two adjacent countries have the same color?

Notice that we define adjacent regions as those that share a common boundary of non-zero length. Regions which meet at a single point are not considered to be "adjacent".

After examining a wide variety of different maps, one discovers the apparent fact that every map, regardless of size or complexity, can be colored with just four distinct colors. This "four-color conjecture" was first noted by August Ferdinand Mobius in 1840. In 1852 a young man named Francis Guthrie wrote about the problem in a letter to his brother Frederick, then a student at University College in London. Neither of the brothers was able to prove the conjecture, so Frederick asked one of his professors, Augustus DeMorgan (1806-1871). DeMorgan too was unable to prove the conjecture, and after recognizing the difficulty of the problem, he wrote to Sir William Rowan Hamilton (1805-1865) to ask for help.

In Greek mythology, the Sirens were sisters whose song lured sailors to their deaths on a treacherous reef. The Four Colour Theorem is to mathematicians what the song of the Sirens was to the sailors of ancient times. Many a mathematician has foundered in attempting its proof.

The four-color map theorem was proved by Appel and Haken at the University of Illinois at Urbana-Champaign in 1976.

Four color mapping has solved complex problems of air traffic control as well as the designing of circuit boards for computers.

now try to color the following maps with no more than four colors.

an example of four coloring the United States is on the next page





















